

Codification et Représentation de l'Information (CRI)

MI – USTHB – TD

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Exercice 1

1- Etablir les tables de vérité des fonctions suivantes :

$$F1 = (X + Y)(\bar{X} + Y + Z)$$

$$F2 = (\bar{X}Y + X\bar{Y})\bar{Z} + (\bar{X}\bar{Y} + XY)Z$$

2- Démontrer à l'aide de tables de vérité les équivalences suivantes :

$$X + YZ = (X + Y)(X + Z)$$

$$(\bar{X} + Y)(X + Z)(Y + Z) = (\bar{X} + Y)(X + Z)$$

| X | Y | Z | \bar{X} | X+Y | $\bar{X}+Y+Z$ | F1 |
|---|---|---|-----------|-----|---------------|----|
| 0 | 0 | 0 | 1 | 0 | 1 | 0 |
| 0 | 0 | 1 | 1 | 0 | 1 | 0 |
| 0 | 1 | 0 | 1 | 1 | 1 | 1 |
| 0 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 0 | 0 | 0 | 1 | 0 | 0 |
| 1 | 0 | 1 | 0 | 1 | 1 | 1 |
| 1 | 1 | 0 | 0 | 1 | 1 | 1 |
| 1 | 1 | 1 | 0 | 1 | 1 | 1 |

Exercice 1

1- Etablir les tables de vérité des fonctions suivantes :

$$F1 = (X + Y)(\bar{X} + Y + Z)$$

$$F2 = (\bar{X}Y + X\bar{Y})\bar{Z} + (\bar{X}\bar{Y} + XY)Z$$

| X | Y | Z | \bar{X} | \bar{Y} | \bar{Z} | $\bar{X}Y$ | $X\bar{Y}$ | $\bar{X}Y + X\bar{Y}$ | $(\bar{X}Y + X\bar{Y})\bar{Z}$ | $\bar{X}\bar{Y}$ | XY | $\bar{X}\bar{Y} + XY$ | $(\bar{X}\bar{Y} + XY)Z$ | F2 |
|---|---|---|-----------|-----------|-----------|------------|------------|-----------------------|--------------------------------|------------------|------|-----------------------|--------------------------|----|
| 0 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 0 | 0 |
| 0 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 1 | 1 |
| 0 | 1 | 0 | 1 | 0 | 1 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 1 |
| 0 | 1 | 1 | 1 | 0 | 0 | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 0 | 0 | 1 | 1 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 1 |
| 1 | 0 | 1 | 0 | 1 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 1 | 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 |
| 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 |

Exercice 1

2- Démontrer à l'aide de tables de vérité les équivalences suivantes :

$$X + YZ = (X+Y)(X+Z)$$

$$(\bar{X} + Y)(X + Z)(Y + Z) = (\bar{X} + Y)(X + Z)$$

$$PG = (\bar{X} + Y)(X + Z)(Y + Z) \quad PD = (\bar{X} + Y)(X + Z)$$

| X | Y | Z | \bar{X} | $\bar{X} + Y$ | X+Z | Y + Z | PG | $(\bar{X} + Y)$ | PD |
|---|---|---|-----------|---------------|-----|-------|----|-----------------|----|
| 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | 0 |
| 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 0 | 1 | 0 | 1 | 1 | 0 | 1 | 0 | 1 | 0 |
| 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| 1 | 0 | 1 | 0 | 0 | 1 | 1 | 0 | 0 | 0 |
| 1 | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 0 | 1 | 1 | 1 | 1 | 1 | 1 |

Exercice 2

Simplifier algébriquement les expressions suivantes :

$$(x + \bar{y} + x \bar{y})(xy + \bar{x}z + yz)$$

$$(x + y + z)(\bar{x} + y + z) + xy + yz$$

$$abcd + abchg + \bar{d}hg + abcdefh.$$

$$a\bar{c}de + \bar{d} + \bar{e} + c$$

Démontrer algébriquement les égalités suivantes :

$$A\bar{B} + \bar{A}\bar{C}\bar{D} + \bar{A}\bar{B}D + \bar{A}\bar{B}C\bar{D} = \bar{A}\bar{C}\bar{D} + \bar{B}$$

$$A.B + \bar{A}.C + B.C = A.B + \bar{A}.C$$

$$AB + ACD + \bar{B}D = AB + \bar{B}D$$

$$AB + \bar{B}C = (A + \bar{B})(B + C)$$

Exercice 2

Simplifier algébriquement les expressions suivantes :

$$1- (x + \bar{y} + x \bar{y})(xy + \bar{x}z + \underline{yz}) \quad \text{//} \quad yz = yz(x + \bar{x})$$

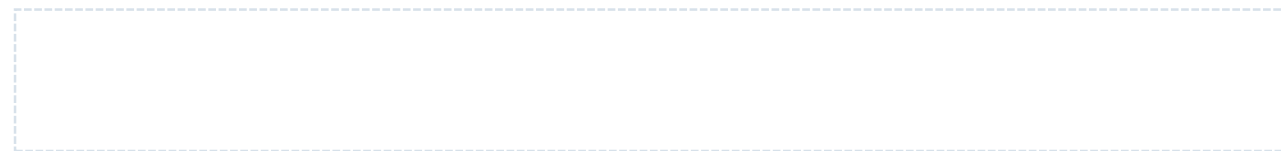
$$\text{// } xy + \bar{x}z + yz = xy + \bar{x}z + \cancel{xyz} + \cancel{yz\bar{x}} = xy + \bar{x}z$$

$$= (x(\cancel{1 + \bar{y}}) + \bar{y})(xy + \bar{x}z)$$

$$= xx\bar{y} + x\bar{x}z + xy\bar{y} + \bar{x}\bar{y}z$$

$$= xy + \cancel{x\bar{x}z} + \cancel{xy\bar{y}} + \bar{x}\bar{y}z$$

$$= xy + \bar{x}\bar{y}z$$



Exercice 2

Simplifier algébriquement les expressions suivantes :

$$2- (x + y + z)(\bar{x} + y + z) + xy + yz$$

$$// (a+b)(a+c) = a + (b.c)$$

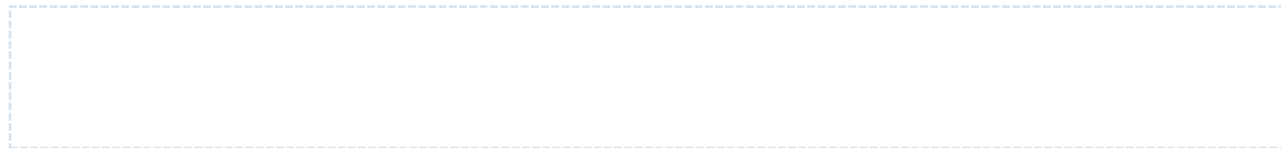
$$\begin{array}{cccc} \underbrace{\quad} & \underbrace{\quad} & \underbrace{\quad} & \underbrace{\quad} \\ \boxed{\mathbf{b}} & \boxed{\mathbf{a}} & \boxed{\mathbf{c}} & \boxed{\mathbf{a}} \end{array}$$

$$= ((y+z) + \cancel{(x\bar{x})}) + xy + yz$$

$$= y+z + xy + yz$$

$$= y(1+x+z) + z$$

$$= y + z$$



Exercice 2

Simplifier algébriquement les expressions suivantes :

$$abcd + abchg + \bar{d}hg + abcdefh.$$

$$= abcd(\cancel{1+efh}) + abchg + \bar{d}hg$$

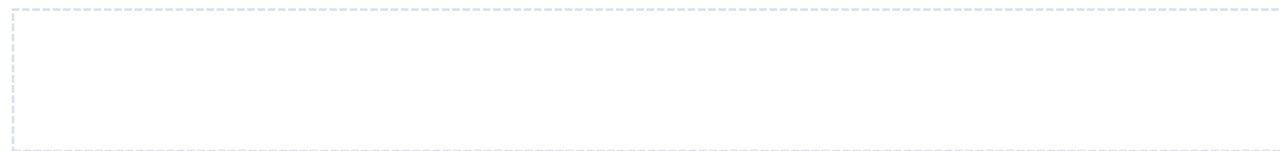
$$= abcd + abchg + \bar{d}hg$$

$$/// abchg(d+/d)$$

$$= abcd + abchg\mathbf{d} + abchg\mathbf{\bar{d}} + \bar{d}hg$$

$$= abcd(\cancel{1+hg}) + hg\bar{d}(\cancel{1+abc})$$

$$= abcd + \bar{d}hg$$



Exercice 2

Simplifier algébriquement les expressions suivantes : // $a + \bar{a} b = a + b$

$$a\bar{c}de + \bar{d} + \bar{e} + c$$

$$= c + \bar{c}ade + \bar{d} + \bar{e} \quad // c + \bar{c}ade = c + ade$$

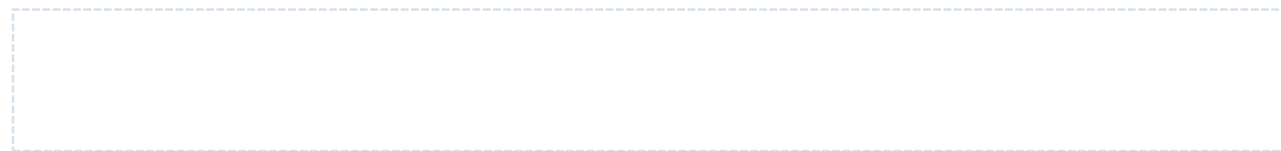
$$= c + ade + \bar{d} + \bar{e}$$

$$= \bar{d} + d\bar{a}e + c + \bar{e} \quad // \bar{d} + d\bar{a}e = \bar{d} + \bar{a}e$$

$$= \bar{d} + \bar{a}e + c + \bar{e}$$

$$= \bar{e} + e\bar{a} + c + \bar{d} \quad // \bar{e} + e\bar{a} = \bar{e} + \bar{a}$$

$$= \bar{e} + \bar{a} + c + \bar{d}$$



Exercice 2

Démontrer algébriquement les égalités suivantes :

$$A \bar{B} + \bar{A} \bar{C} \bar{D} + \bar{A} \bar{B} D + \bar{A} \bar{B} C \bar{D} = \bar{A} \bar{C} \bar{D} + \bar{B}$$

$$A.B + \bar{A}.C + B.C = A.B + \bar{A}.C$$

$$AB + ACD + \bar{B}D = AB + \bar{B}D$$

$$AB + \bar{B}C = (A + \bar{B})(B + C)$$



Exercice 2

Démontrer algébriquement les égalités suivantes :

$$A \bar{B} + \bar{A} \bar{C} \bar{D} + \bar{A} \bar{B} D + \bar{A} \bar{B} C \bar{D} = \bar{A} \bar{C} \bar{D} + \bar{B}$$

$$= A \bar{B} + \bar{A} \bar{C} \bar{D} (B + \bar{B}) + \bar{A} \bar{B} D + \bar{A} \bar{B} C \bar{D}$$

$$= \mathbf{A \bar{B}} + \bar{A} \bar{C} \bar{D} \mathbf{B} + \mathbf{A \bar{C} \bar{D} \bar{B}} + \bar{A} \bar{B} D + \bar{A} \bar{B} C \bar{D}$$

$$= \bar{B} (A + \bar{A} \bar{C} \bar{D} + \bar{A} D + \bar{A} C \bar{D}) + \bar{A} \bar{C} \bar{D} B$$

$$= \bar{B} (A + \cancel{\bar{A} \bar{C} \bar{D}} + \cancel{\bar{A} D} + \cancel{\bar{A} C \bar{D}}) + \bar{A} \bar{C} \bar{D} B$$

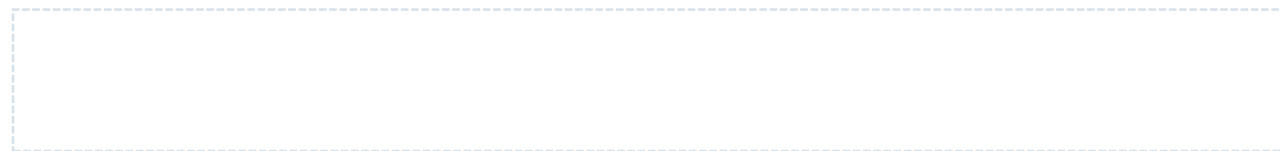
$$= \bar{B} (A + \cancel{\bar{C} \bar{D}} + D + C \cancel{\bar{D}}) + \bar{A} \bar{C} \bar{D} B$$

$$= \bar{B} (A + \bar{C} + D + C) + \bar{A} \bar{C} \bar{D} B$$

$$= \bar{B} (A + D + 1) + \bar{A} \bar{C} \bar{D} B$$

$$= \bar{B} + \bar{A} \bar{C} \bar{D} B$$

$$= \bar{B} + \bar{A} \bar{C} \bar{D}$$



Exercice 2

Démontrer algébriquement les égalités suivantes :

$$A.B + \bar{A}.C + B.C = A.B + \bar{A}.C$$

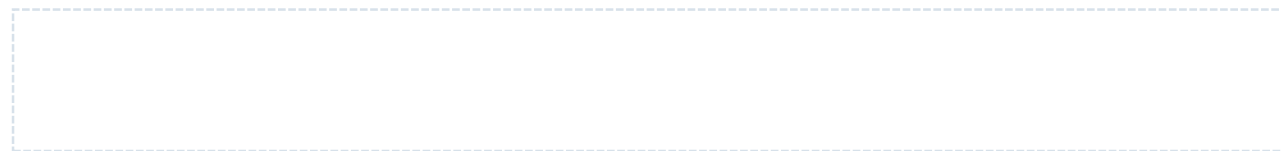
$$= AB + \bar{A}C + BC (A + \bar{A})$$

$$= AB + \bar{A}C + ABC + \bar{A}CB$$

$$// \quad a + ab = a$$

$$= AB(1 + C) + \bar{A}C(1 + B)$$

$$= A.B + \bar{A}.C$$



Exercice 2

Démontrer algébriquement les égalités suivantes :

$$AB + ACD + \bar{B}D = AB + \bar{B}D$$

$$= AB + ACD(\mathbf{B + \bar{B}}) + \bar{B}D$$

$$= AB + ACDB + ACD\bar{B} + \bar{B}D \quad // \quad a + ab = a$$

$$= AB + \bar{B}D$$

Exercice 2

Démontrer algébriquement les égalités suivantes :

$$AB + \bar{B}C = (A + \bar{B})(B + C)$$

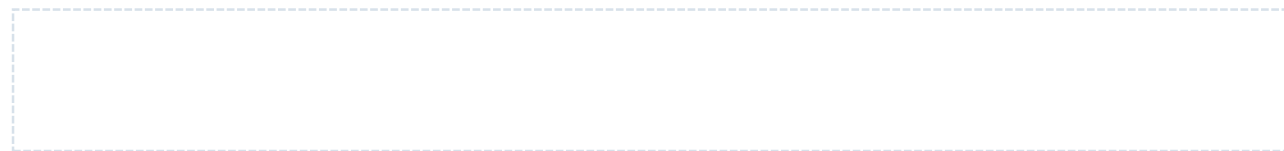
$$(A + \bar{B})(B + C) = AB + AC + \cancel{B\bar{B}} + \bar{B}C$$

$$= AB + AC(B + \bar{B}) + \bar{B}C$$

$$= AB + ACB + AC\bar{B} + \bar{B}C$$

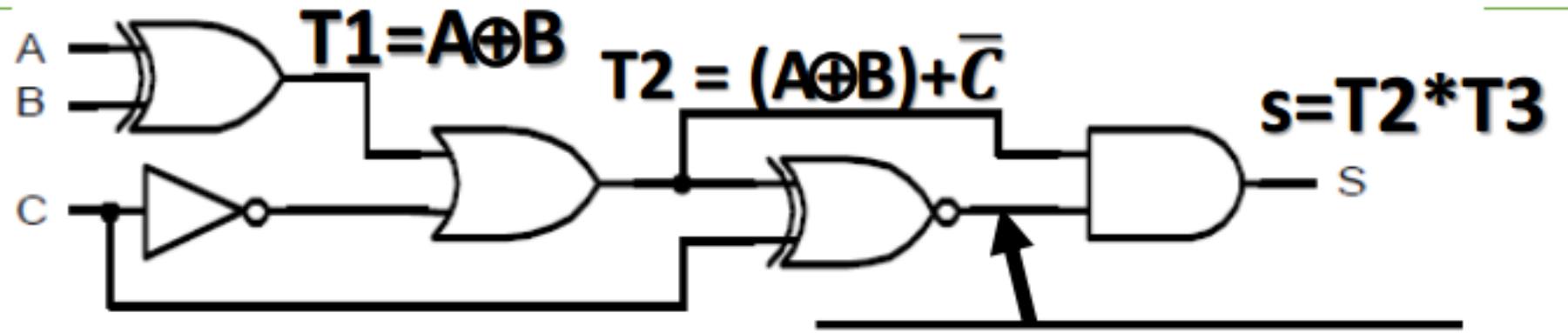
$$= AB(\cancel{1+C}) + \bar{B}C(\cancel{1+A})$$

$$= AB + \bar{B}C$$



Exercise 4

Exercise 4 :



| A | B | C | T1 | T2 | T3 | S |
|---|---|---|----|----|----|---|
| 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| 0 | 1 | 0 | 1 | 1 | 0 | 0 |
| 0 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 0 | 0 | 1 | 1 | 0 | 0 |
| 1 | 0 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 0 | 0 | 1 | 0 | 0 |
| 1 | 1 | 1 | 0 | 0 | 0 | 0 |

$$F(a,b,c) = \bar{a}bc + a\bar{b}c$$

$$\bar{F}(a,b,c) = \bar{a}/b/c + /a/\bar{b}c + \dots$$

Exo 5 - 1

| ab cd , | 00 | 01 | 11 | 10 |
|------------|----|----|----|----|
| 00 | 1 | 1 | 1 | |
| 01 | | 1 | 1 | |
| 11 | | 1 | 1 | |
| 10 | 1 | 1 | 1 | 1 |

$$F(a,b,c,d) = \bar{a}\bar{d} + b + c\bar{d}$$

La forme disjonctive

Exo 5 - 1

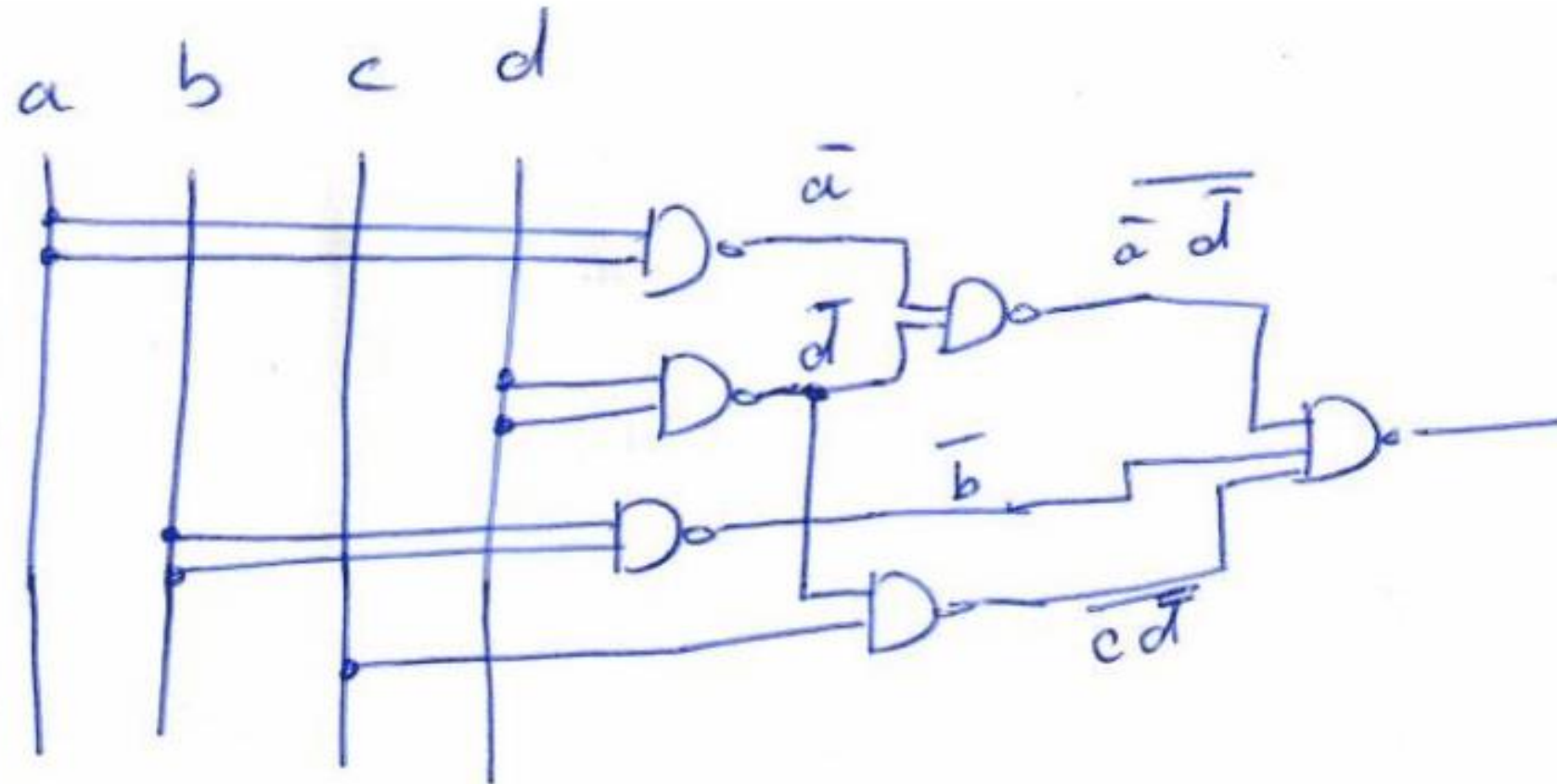
$$F(a,b,c,d) = \bar{a}\bar{d} + b + c\bar{d}$$

$$F(a,b,c,d) = \overline{\bar{a}\bar{d} + b + c\bar{d}}$$

$$F(a,b,c,d) = \overline{\bar{a}\bar{d}} \cdot \bar{b} \cdot \overline{c\bar{d}}$$

Exo 5 - 1

$$F(a,b,c,d) = \overline{\overline{a} \overline{d}} \cdot \overline{b} \cdot \overline{c d}$$



Exo 5 - 1

| ab cd , | 00 | 01 | 11 | 10 |
|------------|----|----|----|----|
| 00 | 1 | 1 | 1 | 0 |
| 01 | 0 | 1 | 1 | 0 |
| 11 | 0 | 1 | 1 | 0 |
| 10 | 1 | 1 | 1 | 1 |

$$\overline{F(a,b,c,d)} = \overline{bd} + a\overline{b}\overline{c}$$

$$F(a,b,c,d) = (b+\overline{d})(\overline{a}+b+c)$$

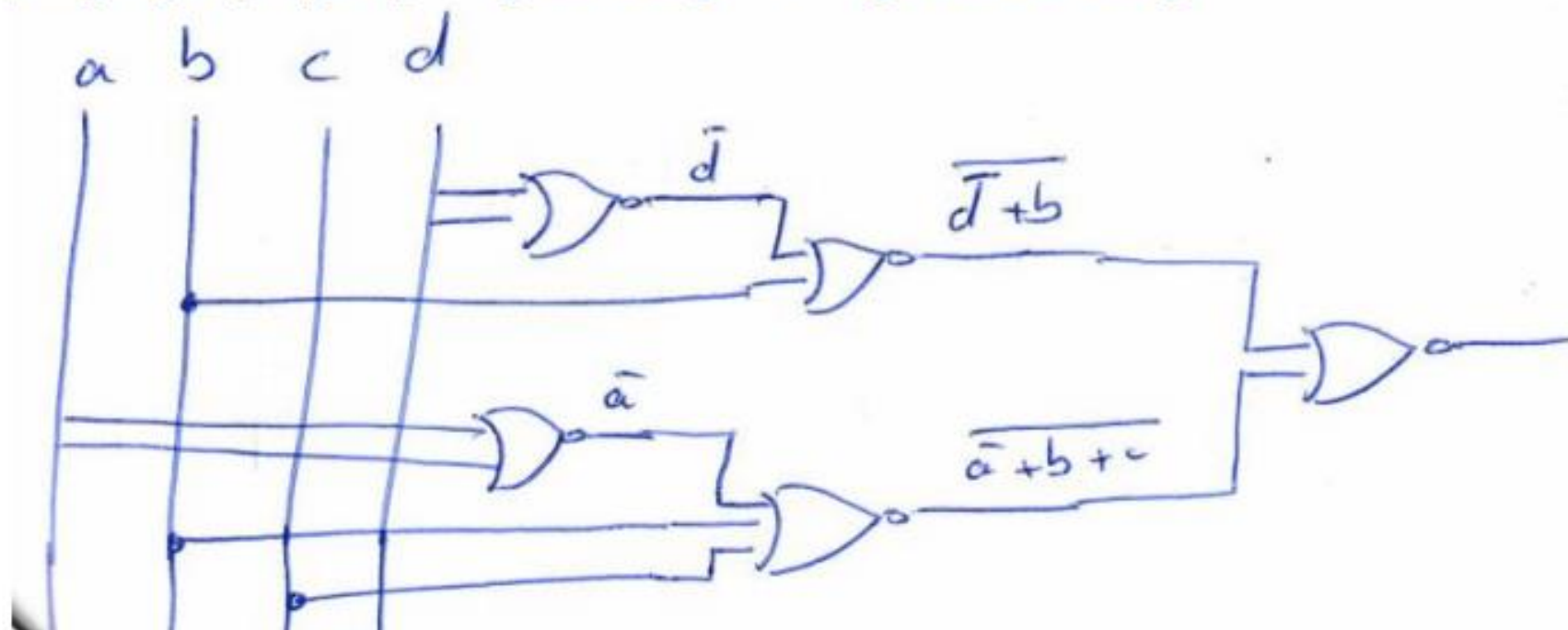
La forme conjonctive

Exo 5 - 1

$$F(a,b,c,d) = (b+\bar{d})(\bar{a}+b+c)$$

$$F(a,b,c,d) = \overline{\overline{(b+\bar{d})(\bar{a}+b+c)}}$$

$$F(a,b,c,d) = \overline{\overline{(b+\bar{d})}} + \overline{\overline{(\bar{a}+b+c)}}$$



Exo 5 - 2

| ab cd , | 00 | 01 | 11 | 10 |
|------------|----|----|----|----|
| 00 | 1 | | | 1 |
| 01 | | 1 | 1 | |
| 11 | | 1 | 1 | |
| 10 | 1 | | | 1 |

$$F(a,b,c,d) = bd + \bar{b}\bar{d}$$

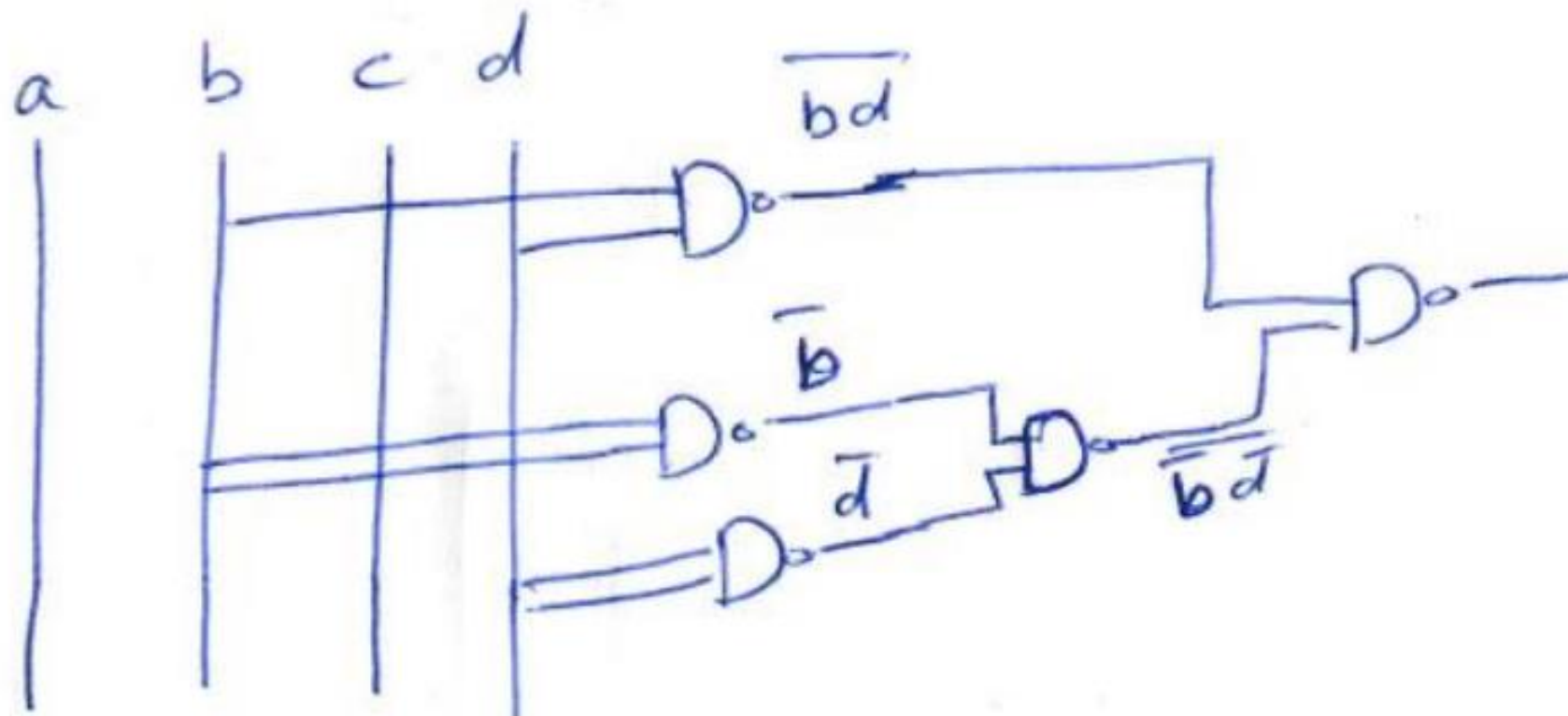
La forme disjonctive

Exo 5 - 2

$$F(a,b,c,d) = bd + \overline{b}\overline{d}$$

$$F(a,b,c,d) = \overline{\overline{bd} + \overline{\overline{b}\overline{d}}}$$

$$F(a,b,c,d) = \overline{\overline{bd} \cdot \overline{\overline{b}\overline{d}}}$$



Exo 5 - 2

| ab cd , | 00 | 01 | 11 | 10 |
|------------|----|----|----|----|
| 00 | 1 | 0 | 0 | 1 |
| 01 | 0 | 1 | 1 | 0 |
| 11 | 0 | 1 | 1 | 0 |
| 10 | 1 | 0 | 0 | 1 |

$$\overline{F(a,b,c,d)} = \bar{b}d + b\bar{d}$$

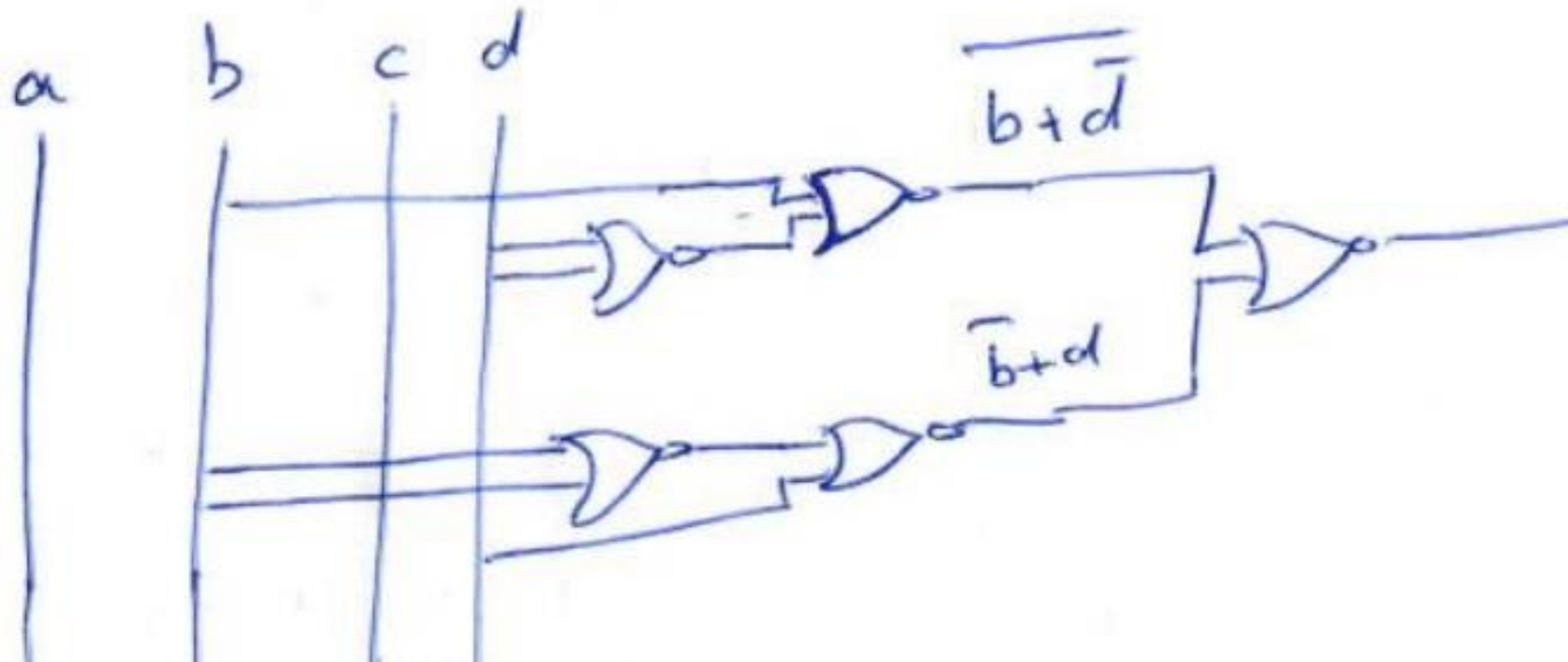
$$F(a,b,c,d) = (b + \bar{d})(\bar{b} + d)$$

La forme conjonctive

Exo 5 - 2

$$F(a,b,c,d) = (b + \bar{d})(\bar{b} + d)$$

$$F(a,b,c,d) = \overline{(b+\bar{d})} \overline{(\bar{b}+d)} = \overline{(b+\bar{d})} + \overline{(\bar{b}+d)}$$



Exercise 5

| cd \ ab | 00 | 01 | 11 | 10 |
|---------|----|----|----|----|
| 00 | 1 | | | 1 |
| 01 | 1 | 1 | | 1 |
| 11 | | 1 | 1 | |
| 10 | 1 | | 1 | 1 |

The table above is a Karnaugh map for a function F(a,b,c,d). The top row and left column are highlighted in yellow. The main body of the map is highlighted in light green. The cell (11, 11) is highlighted in red. The map contains several groupings: a blue dashed circle grouping (00,00), (00,10), (01,00), (01,10); a green dashed circle grouping (01,01), (11,01), (01,11), (11,11); a brown dashed circle grouping (11,11), (10,11), (11,10), (10,10); and two orange solid circles grouping (00,00), (01,00) and (10,10), (11,10).

$$F(a,b,c,d) = \neg b/c + \neg b/d + abd + abc$$

Exercice 5

Exo 5 - 3

$$F(a,b,c,d) = \bar{b}\bar{c} + \bar{b}\bar{d} + \bar{a}bd + abc$$

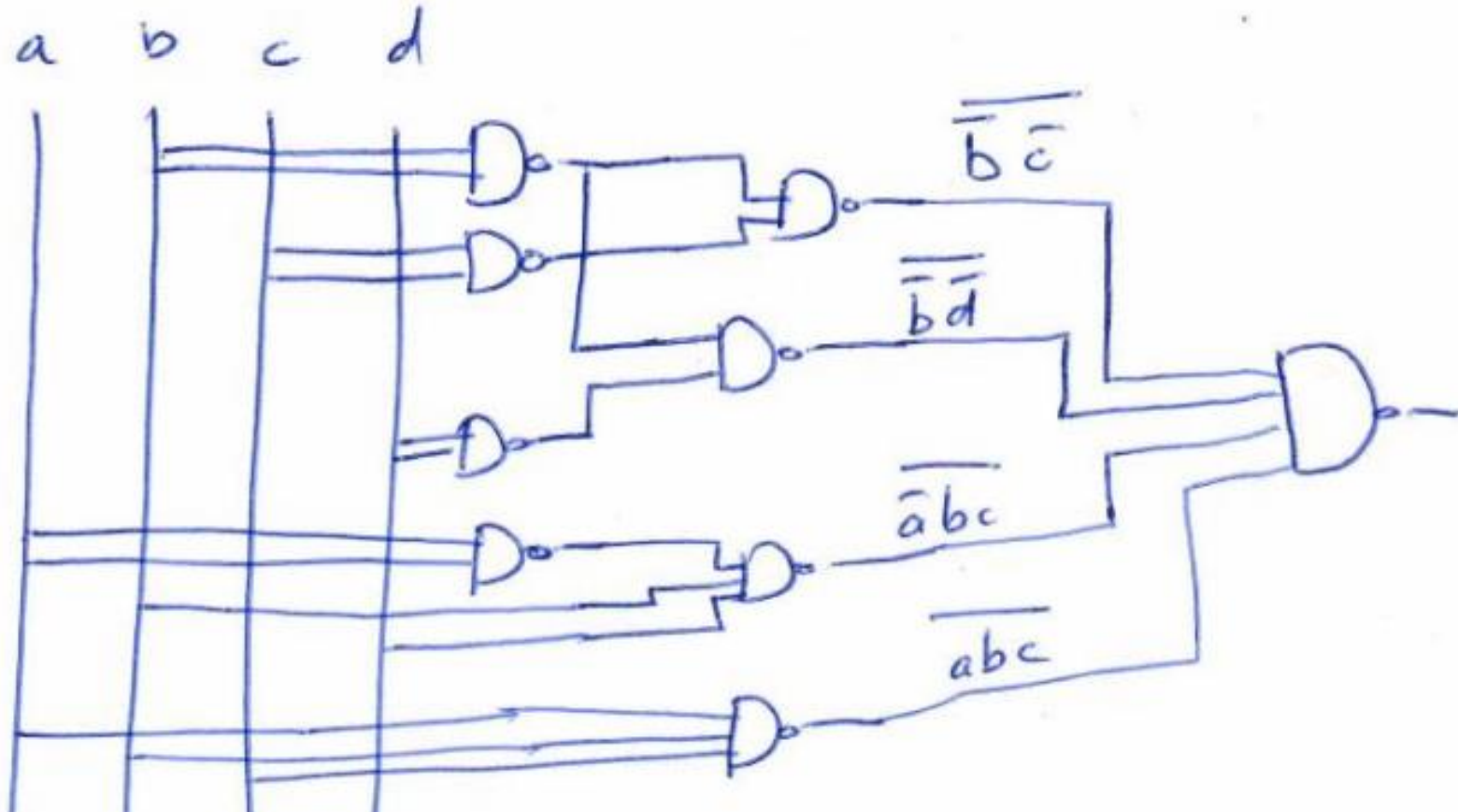
$$F(a,b,c,d) = \overline{\bar{b}\bar{c} + \bar{b}\bar{d} + \bar{a}bd + abc}$$

$$F(a,b,c,d) = \overline{\bar{b}\bar{c}} \cdot \overline{\bar{b}\bar{d}} \cdot \overline{\bar{a}bd} \cdot \overline{abc}$$

Exercice 5

Exo 5 - 3

$$F(a,b,c,d) = \overline{\overline{b\bar{c}}} \cdot \overline{\overline{b\bar{d}}} \cdot \overline{\overline{a\bar{b}d}} \cdot \overline{\overline{abc}}$$



Exercise 5

| ab \ cd | 00 | 01 | 11 | 10 |
|---------|----|----|----|----|
| 00 | 1 | 0 | 0 | 1 |
| 01 | 1 | 1 | 0 | 1 |
| 11 | 0 | 1 | 1 | 0 |
| 10 | 1 | 0 | 1 | 1 |

$$\overline{F}(a,b,c,d) = ab\overline{c} + \overline{ab}d + \overline{bcd}$$

$$F(a,b,c,d) = (\overline{a} + \overline{b} + c)(a + \overline{b} + d)(b + \overline{c} + \overline{d})$$

Exo 5 - 3

$$\overline{F(a,b,c,d)} = \bar{b}cd + \bar{a}b\bar{d} + ab\bar{c}$$

La forme conjonctive

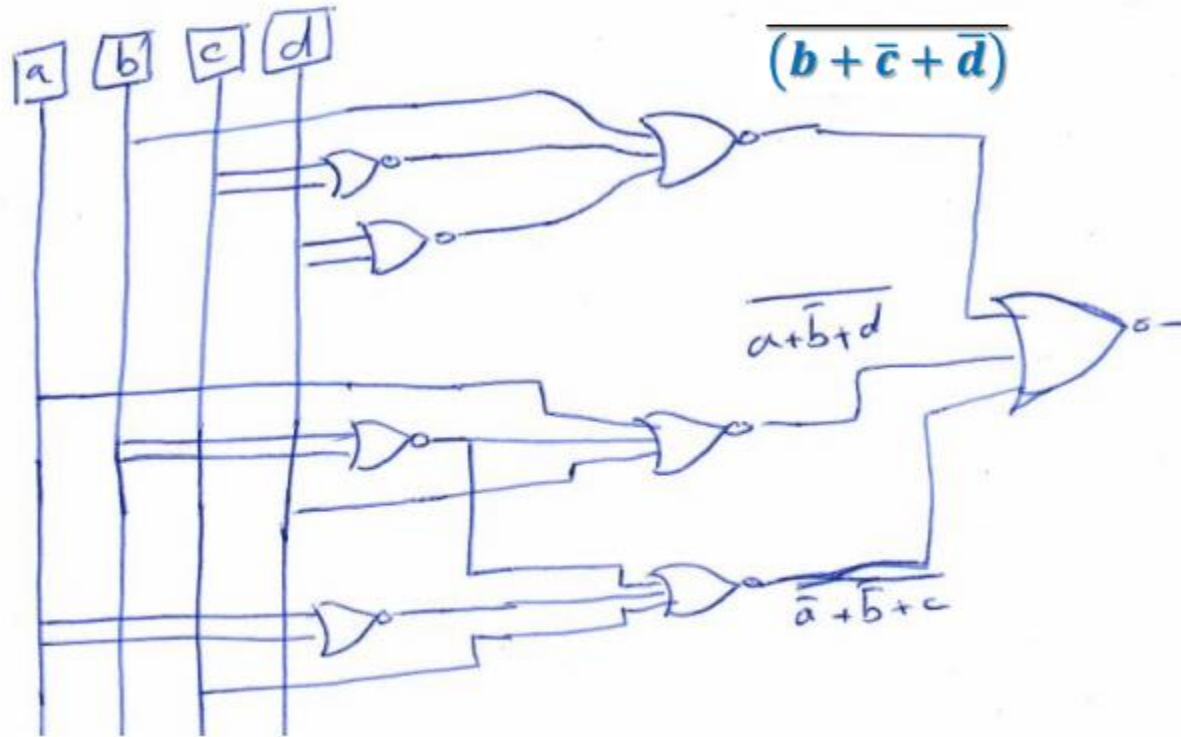
$$F(a,b,c,d) = (b + \bar{c} + \bar{d})(a + \bar{b} + d)(\bar{a} + \bar{b} + c)$$

$$F(a,b,c,d) = \overline{\overline{(b + \bar{c} + \bar{d})(a + \bar{b} + d)(\bar{a} + \bar{b} + c)}}$$

$$F(a,b,c,d) = \overline{\overline{(b + \bar{c} + \bar{d})} + \overline{\overline{(a + \bar{b} + d)}} + \overline{\overline{(\bar{a} + \bar{b} + c)}}}$$

Exo 5 - 3

$$F(a,b,c,d) = \overline{\overline{(b + \bar{c} + \bar{d})}} + \overline{\overline{(a + \bar{b} + d)}} + \overline{\overline{(\bar{a} + \bar{b} + c)}}$$



Exercise 5

| ab \ cd | 00 | 01 | 11 | 10 |
|---------|----|----|----|----|
| 00 | | x | x | 1 |
| 01 | | 1 | 1 | 1 |
| 11 | | 1 | 1 | |
| 10 | | 1 | 1 | |



$$F(a,b,c,d) = b + a/c$$

Exo 5 - 4

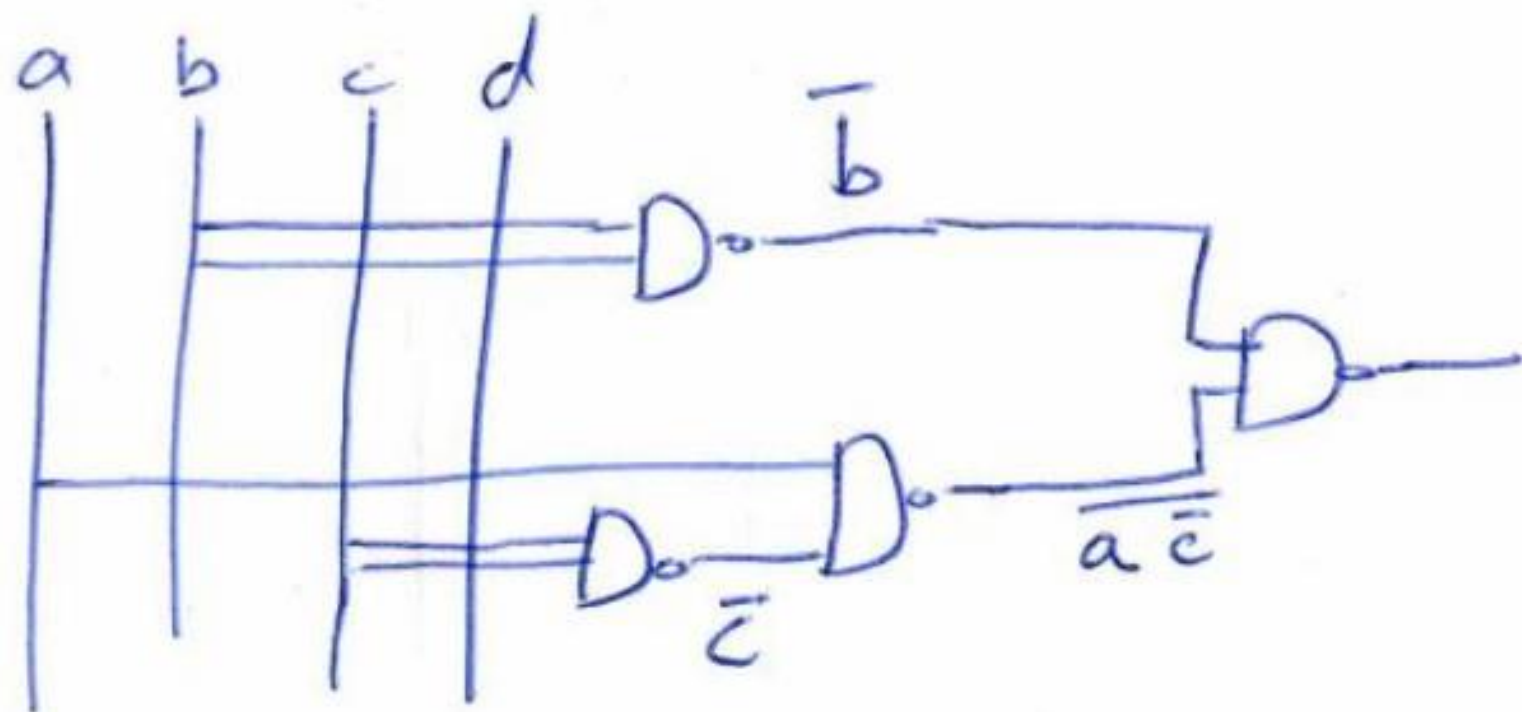
$$F(a,b,c,d) = b + a\bar{c}$$

$$F(a,b,c,d) = \overline{\overline{b} + \overline{a\bar{c}}}$$

$$F(a,b,c,d) = \overline{\overline{b}} \cdot \overline{\overline{a\bar{c}}}$$

Exo 5 - 4

$$F(a,b,c,d) = \overline{\overline{b}} \cdot \overline{\overline{a\overline{c}}}$$



Exercise 5

| cd \ ab | 00 | 01 | 11 | 10 |
|---------|----|----|----|----|
| 00 | 0 | x | x | 1 |
| 01 | 0 | 1 | 1 | 1 |
| 11 | 0 | 1 | 1 | 0 |
| 10 | 0 | 1 | 1 | 0 |

$$/F(a,b,c,d) = /a/b + /bc$$

$$/F(a,b,c,d) = (a+b) (b+/c)$$

Exo 5 - 4

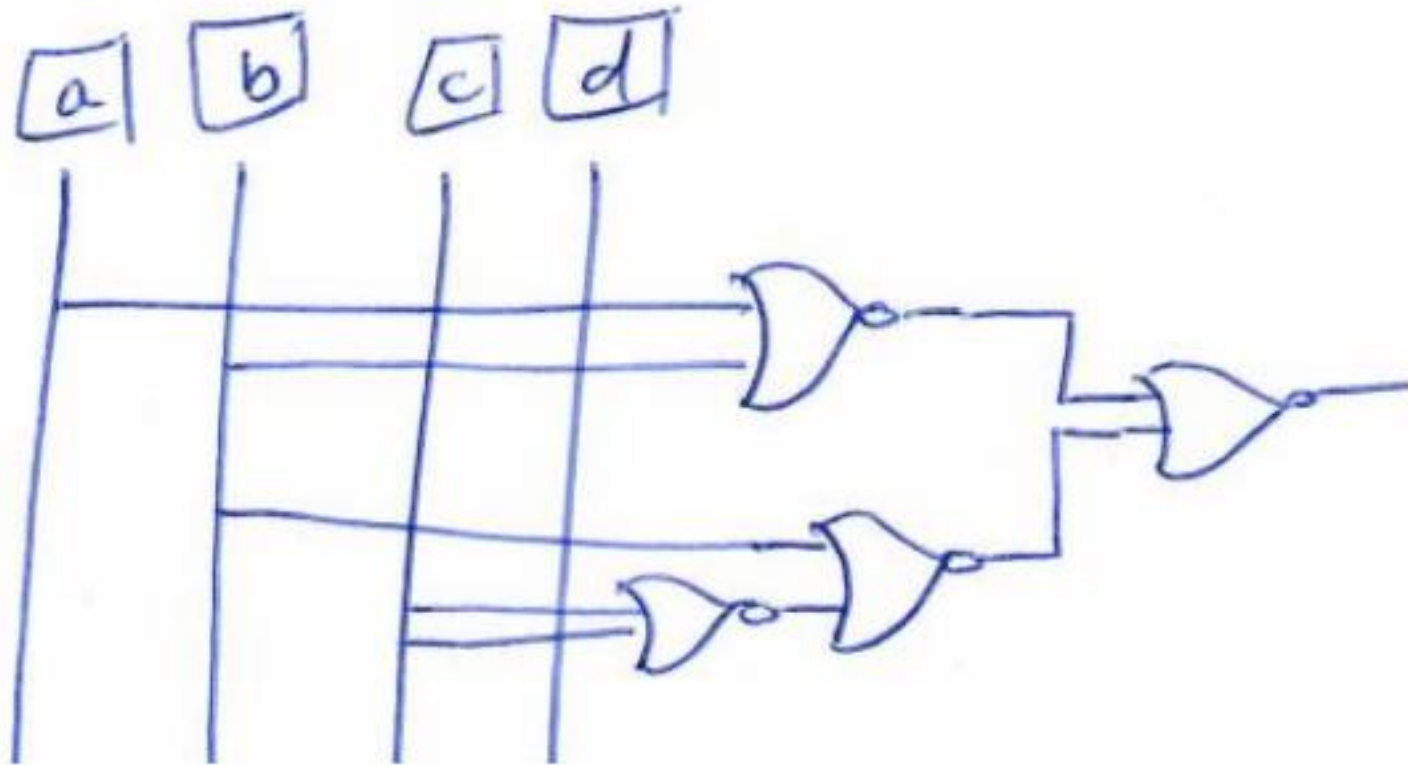
$$F(a,b,c,d) = (a+b)(b+\bar{c})$$

$$F(a,b,c,d) = \overline{\overline{(a+b)(b+\bar{c})}}$$

$$F(a,b,c,d) = \overline{\overline{(a+b)} + \overline{\overline{(b+\bar{c})}}}$$

Exo 5 - 4

$$F(a,b,c,d) = \overline{\overline{(a+b)}} + \overline{\overline{(b+\bar{c})}}$$



Exercise 5

| cd \ ab | 00 | 01 | 11 | 10 |
|---------|----|----|----|----|
| 00 | 1 | | | 1 |
| 01 | X | 1 | 1 | 1 |
| 11 | X | 1 | 1 | x |
| 10 | x | | | |

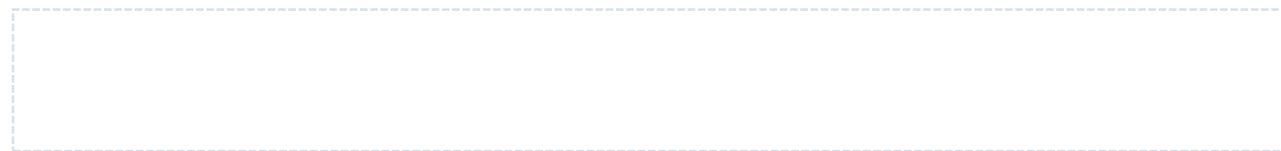
$$F(a,b,c,d) = d + /b/c$$

Exo 5 - 5

$$F(a,b,c,d) = d + \bar{b}\bar{c}$$

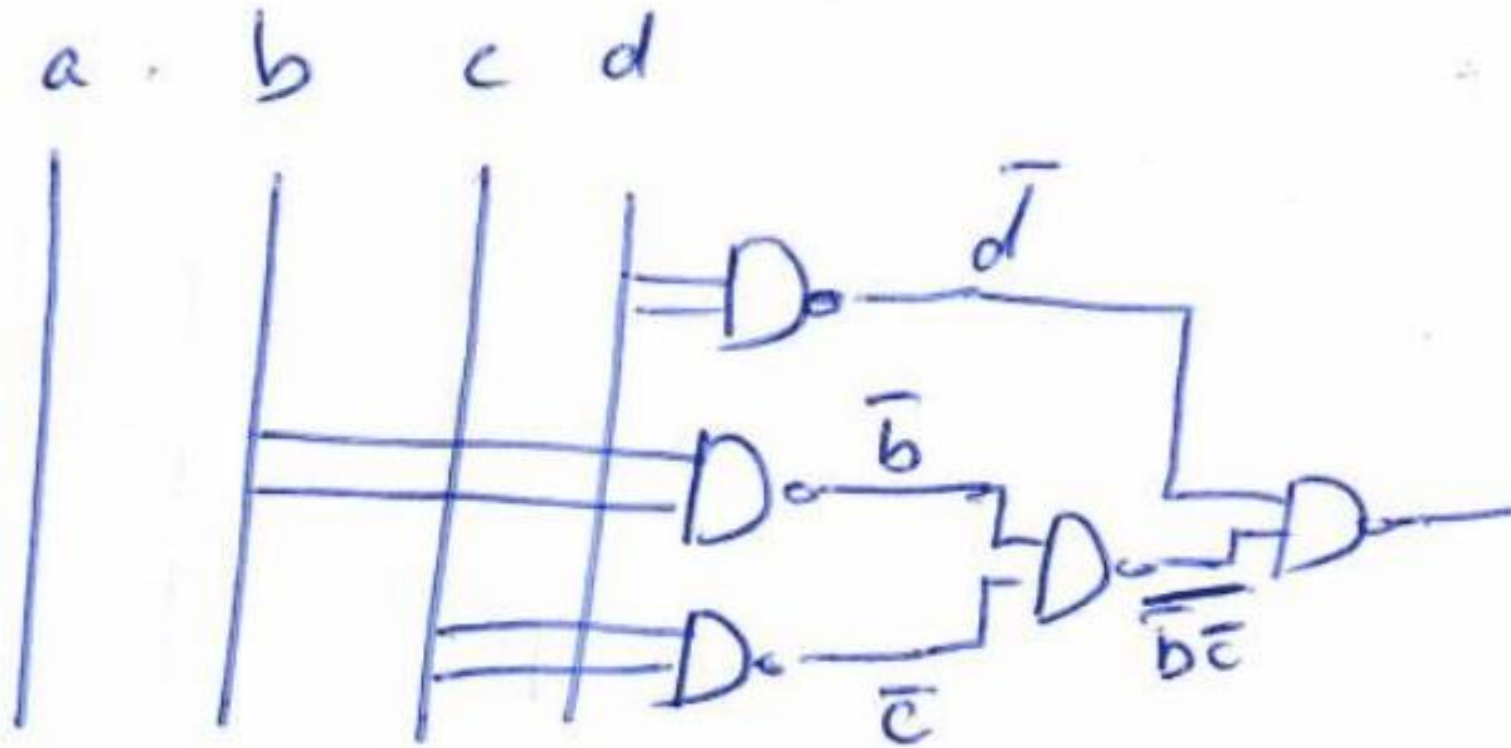
$$F(a,b,c,d) = \overline{\overline{d + \bar{b}\bar{c}}}$$

$$F(a,b,c,d) = \overline{\bar{d}} \cdot \overline{\bar{b}\bar{c}}$$



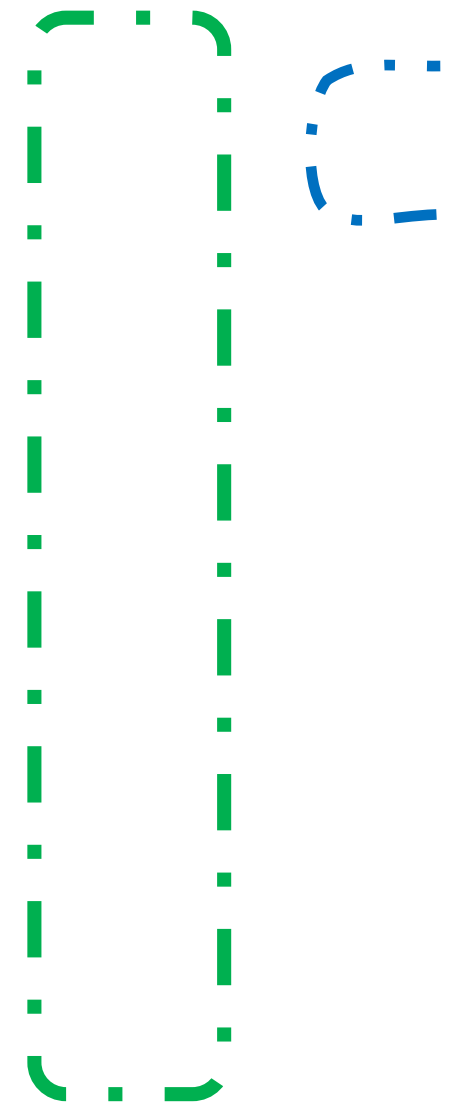
Exo 5 - 5

$$F(a,b,c,d) = \overline{\overline{d}} \cdot \overline{\overline{bc}}$$



Exercise 5

| ab \ cd | 00 | 01 | 11 | 10 |
|---------|----|----|----|----|
| 00 | 1 | 0 | 0 | 1 |
| 01 | X | 1 | 1 | 1 |
| 11 | X | 1 | 1 | x |
| 10 | x | 0 | 0 | 0 |



$$/F(a,b,c,d) = c/d + b/d$$

$$F(a,b,c,d) = (/c+d)(/b+d)$$

Exo 5 - 5

$$\overline{F(a,b,c,d)} = c\bar{d} + b\bar{d}$$

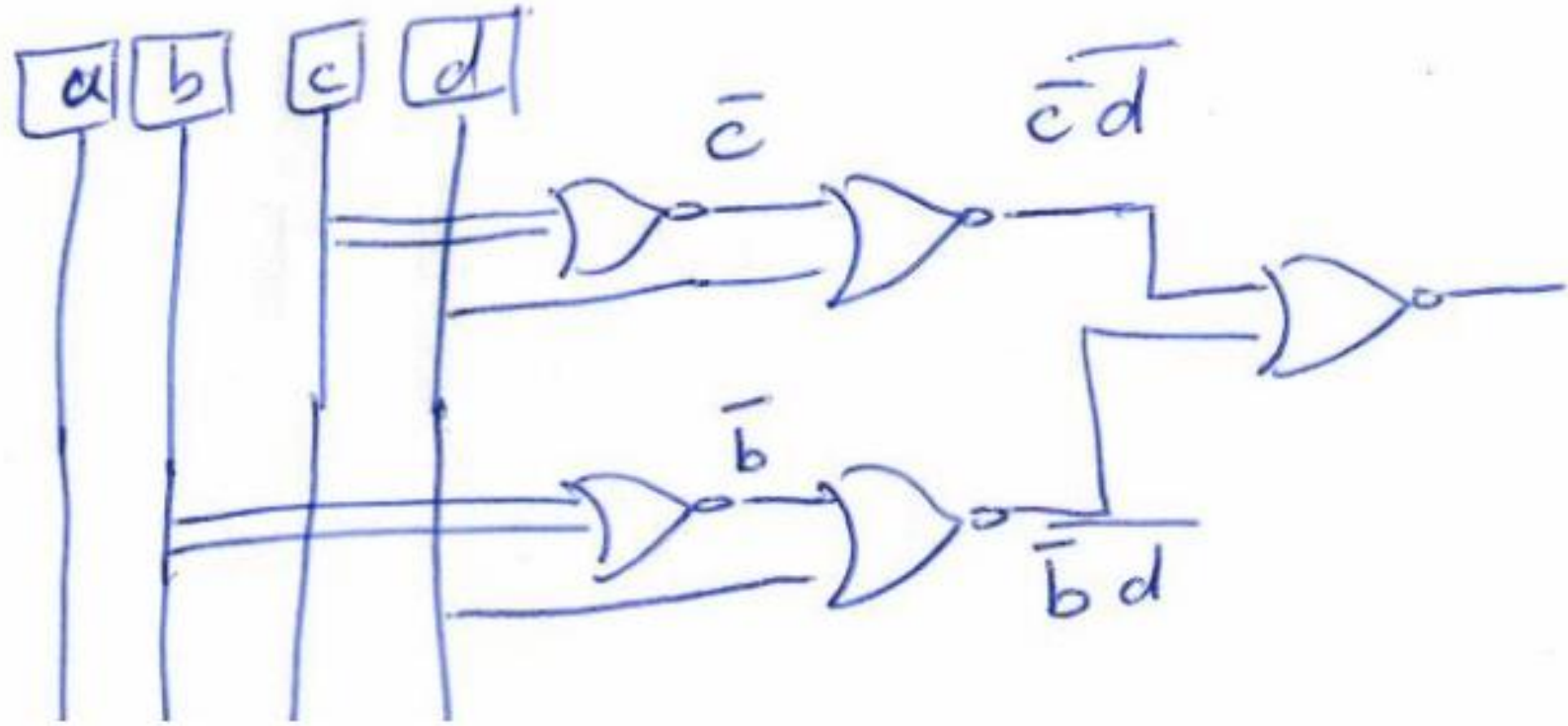
$$F(a,b,c,d) = (\bar{c} + d)(\bar{b} + d) \quad \text{La forme conjonctive}$$

$$F(a,b,c,d) = \overline{(\bar{c} + d)(\bar{b} + d)}$$

$$F(a,b,c,d) = \overline{(\bar{c} + d)} + \overline{(\bar{b} + d)}$$

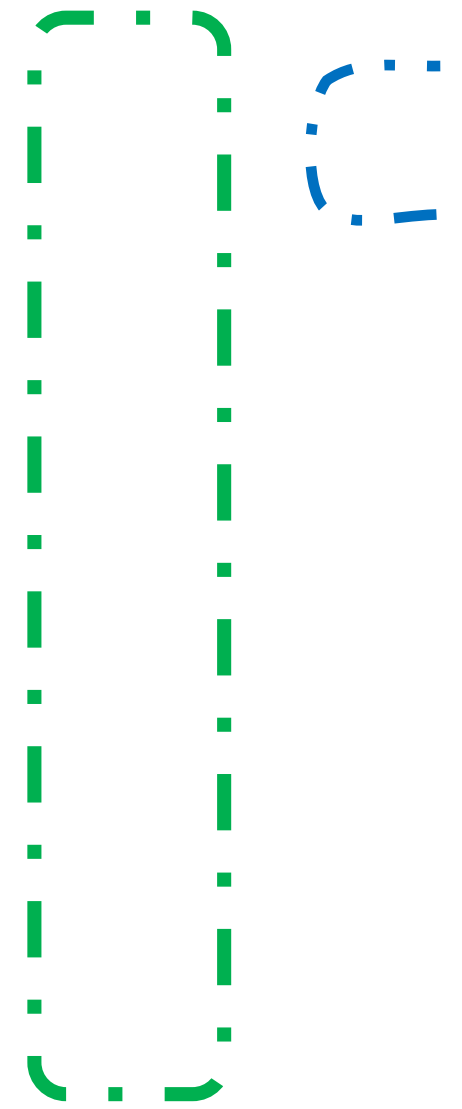
Exo 5 - 5

$$F(a,b,c,d) = \overline{(\bar{c} + d)} + \overline{(\bar{b} + d)}$$



Exercise 5

| ab \ cd | 00 | 01 | 11 | 10 |
|---------|----|----|----|----|
| 00 | 1 | 1 | | 1 |
| 01 | 1 | 1 | x | 1 |
| 11 | 1 | 1 | | 1 |
| 10 | x | x | | |



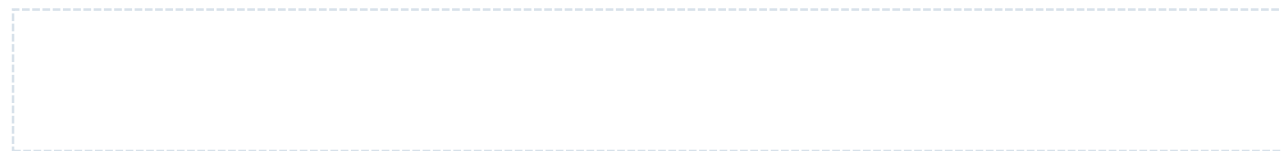
$$F(a,b,c,d) = \bar{a} + \bar{b}/c + \bar{b}d$$

Exo 5 - 6

$$F(a,b,c,d) = \bar{a} + \bar{b}\bar{c} + \bar{b}d$$

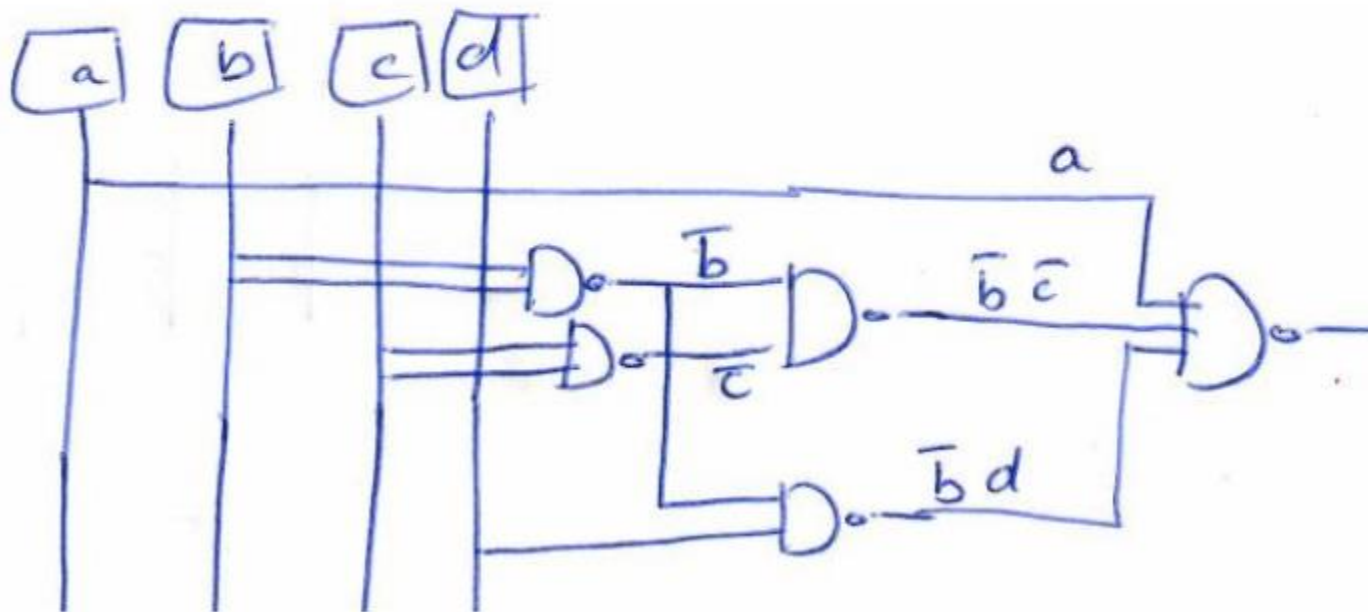
$$F(a,b,c,d) = \overline{\bar{a} + \bar{b}\bar{c} + \bar{b}d}$$

$$F(a,b,c,d) = \overline{\bar{a} \cdot \bar{b}\bar{c} \cdot \bar{b}d}$$



Exo 5 - 6

$$F(a,b,c,d) = \overline{\overline{a}} \cdot \overline{\overline{b\overline{c}}} \cdot \overline{\overline{bd}}$$



Exercise 5

| ab \ cd | 00 | 01 | 11 | 10 |
|---------|----|----|----|----|
| 00 | 1 | 1 | 0 | 1 |
| 01 | 1 | 1 | X | 1 |
| 11 | 1 | 1 | 0 | 1 |
| 10 | x | x | 0 | 0 |



$$\overline{F}(a,b,c,d) = ab + c/d$$

$$F(a,b,c,d) = (\overline{a} + \overline{b}) (\overline{c} + d)$$

Exo 5 - 6

$$F(a,b,c,d) = (\bar{a} + \bar{b})(\bar{c} + d)$$

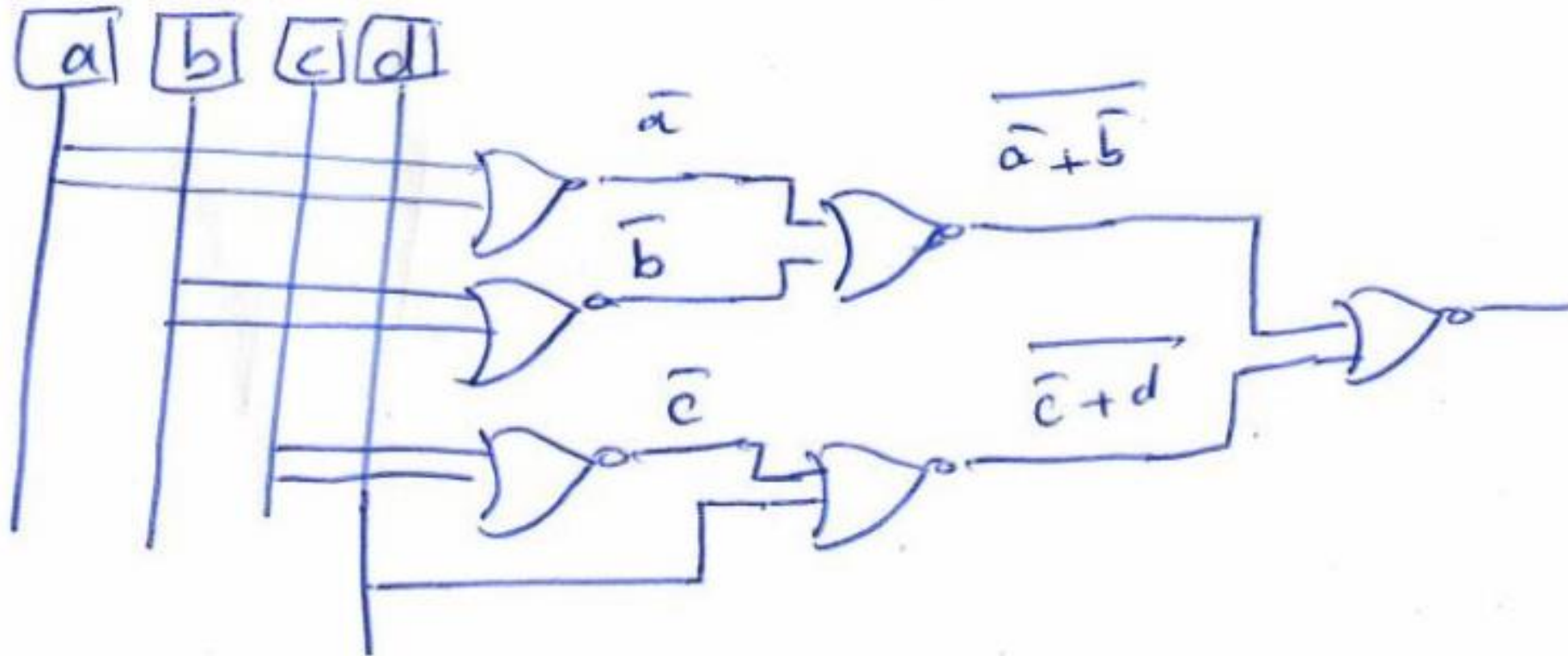
$$F(a,b,c,d) = \overline{\overline{(\bar{a} + \bar{b})(\bar{c} + d)}}$$

$$F(a,b,c,d) = \overline{(\bar{a} + \bar{b})} + \overline{(\bar{c} + d)}$$



Exo 5 - 6

$$F(a,b,c,d) = \overline{\overline{(\bar{a} + \bar{b})} + \overline{(\bar{c} + d)}}$$



Simplifier à l'aide du Tableau de Karnaugh les fonctions suivantes

puis réaliser les circuits correspondants à l'aide de portes NOR ou NAND.

$$F(a, b, c) = \pi(0, 1, 2, 3, 4, 7)$$

$$G(a, b, c, d) = \sum(2, 6, 7, 10, 11, 12, 14)$$

$$F(a, b, c) = \pi(0, 1, 2, 3, 4, 7)$$

//positions de 0

$$G(a, b, c, d) = \Sigma(2, 6, 7, 10, 11, 12, 14)$$

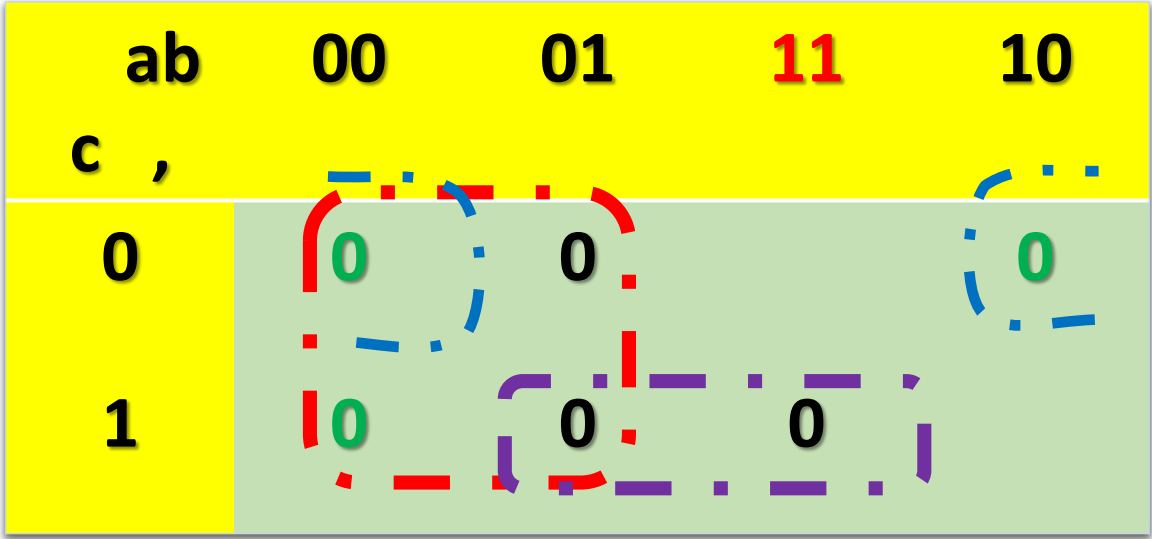
// positions de 1

| | <i>a</i> | <i>b</i> | <i>c</i> | F |
|----------|----------|----------|----------|---|
| <u>0</u> | 0 | 0 | 0 | 0 |
| <u>1</u> | 0 | 0 | 1 | 0 |
| <u>2</u> | 0 | 1 | 0 | 0 |
| <u>3</u> | 0 | 1 | 1 | 0 |
| <u>4</u> | 1 | 0 | 0 | 0 |
| <u>5</u> | 1 | 0 | 1 | 1 |
| <u>6</u> | 1 | 1 | 0 | 1 |
| <u>7</u> | 1 | 1 | 1 | 0 |

| | <i>a</i> | <i>b</i> | <i>c</i> | <i>d</i> | G |
|-----------|----------|----------|----------|----------|---|
| <u>0</u> | 0 | 0 | 0 | 0 | 0 |
| <u>1</u> | 0 | 0 | 0 | 1 | 1 |
| <u>2</u> | 0 | 0 | 1 | 0 | 0 |
| <u>3</u> | 0 | 0 | 1 | 1 | 0 |
| <u>4</u> | 0 | 1 | 0 | 0 | 0 |
| <u>5</u> | 0 | 1 | 0 | 1 | 0 |
| <u>6</u> | 0 | 1 | 1 | 0 | 1 |
| <u>7</u> | 0 | 1 | 1 | 1 | 1 |
| <u>8</u> | 1 | 0 | 0 | 0 | 0 |
| <u>9</u> | 1 | 0 | 0 | 1 | 0 |
| <u>10</u> | 1 | 0 | 1 | 0 | 1 |
| <u>11</u> | 1 | 0 | 1 | 1 | 1 |
| <u>12</u> | 1 | 1 | 0 | 0 | 1 |
| <u>13</u> | 1 | 1 | 0 | 1 | 0 |
| <u>14</u> | 1 | 1 | 1 | 0 | 1 |
| <u>15</u> | 1 | 1 | 1 | 1 | 0 |

$$F(a, b, c) = \pi(0, 1, 2, 3, 4, 7)$$

| | <i>a</i> | <i>b</i> | <i>c</i> | F |
|----------|----------|----------|----------|---|
| <u>0</u> | 0 | 0 | 0 | 0 |
| <u>1</u> | 0 | 0 | 1 | 0 |
| <u>2</u> | 0 | 1 | 0 | 0 |
| <u>3</u> | 0 | 1 | 1 | 0 |
| <u>4</u> | 1 | 0 | 0 | 0 |
| <u>5</u> | 1 | 0 | 1 | 1 |
| <u>6</u> | 1 | 1 | 0 | 1 |
| <u>7</u> | 1 | 1 | 1 | 0 |



$$F(a,b,c) = ab/c + a/bc$$

$$\overline{F}(a,b,c) = \overline{a} + \overline{b}/c + bc$$

$$F(a,b,c) = a (b+c) (\overline{b}+c)$$

Exo 6

$$F(a, b, c) = \pi(0, 1, 2, 3, 4, 7)$$

$$F(a, b, c) = \overline{a}b\overline{c} + a\overline{b}c$$

$$F(a, b, c) = \overline{\overline{a}b\overline{c}} \cdot \overline{\overline{a\overline{b}c}}$$

$$\overline{F(a,b,c)} = \bar{a} + bc + \bar{b}\bar{c} \quad F(a,b,c) = a(b+c)(\bar{b} + \bar{c})$$

Exo 6

$$F(a, b, c) = \pi(0, 1, 2, 3, 4, 7)$$

$$F(a,b,c) = \overline{\overline{a(b+c)(\bar{b} + \bar{c})}}$$

$$F(a,b,c) = \bar{a} + \overline{(b+c)} + \overline{(\bar{b} + \bar{c})}$$

$$G(a, b, c, d) = \sum(2, 6, 7, 10, 11, 12, 14)$$

| ab \ cd | 00 | 01 | 11 | 10 |
|---------|----|----|----|----|
| 00 | 0 | 0 | 1 | 0 |
| 01 | 0 | 0 | 0 | 0 |
| 11 | 0 | 1 | 0 | 1 |
| 10 | 1 | 1 | 1 | 1 |

| | a | b | c | d | G |
|-----------|---|---|---|---|---|
| <u>0</u> | 0 | 0 | 0 | 0 | 0 |
| <u>1</u> | 0 | 0 | 0 | 1 | 0 |
| <u>2</u> | 0 | 0 | 1 | 0 | 1 |
| <u>3</u> | 0 | 0 | 1 | 1 | 0 |
| <u>4</u> | 0 | 1 | 0 | 0 | 0 |
| <u>5</u> | 0 | 1 | 0 | 1 | 0 |
| <u>6</u> | 0 | 1 | 1 | 0 | 1 |
| <u>7</u> | 0 | 1 | 1 | 1 | 1 |
| <u>8</u> | 1 | 0 | 0 | 0 | 0 |
| <u>9</u> | 1 | 0 | 0 | 1 | 0 |
| <u>10</u> | 1 | 0 | 1 | 0 | 1 |
| <u>11</u> | 1 | 0 | 1 | 1 | 1 |
| <u>12</u> | 1 | 1 | 0 | 0 | 1 |
| <u>13</u> | 1 | 1 | 0 | 1 | 0 |
| <u>14</u> | 1 | 1 | 1 | 0 | 1 |

$$G(a,b,c,d) = c/d + ab/d + \overline{a}bc + a/\overline{b}c$$

$$G(a, b, c, d) = \sum(2, 6, 7, 10, 11, 12, 14)$$

| ab \ cd | 00 | 01 | 11 | 10 |
|---------|----|----|----|----|
| 00 | 0 | 0 | 1 | 0 |
| 01 | 0 | 0 | 0 | 0 |
| 11 | 0 | 1 | 0 | 1 |
| 10 | 1 | 1 | 1 | 1 |

| | a | b | c | d | G |
|-----------|---|---|---|---|---|
| <u>0</u> | 0 | 0 | 0 | 0 | 0 |
| <u>1</u> | 0 | 0 | 0 | 1 | 0 |
| <u>2</u> | 0 | 0 | 1 | 0 | 1 |
| <u>3</u> | 0 | 0 | 1 | 1 | 0 |
| <u>4</u> | 0 | 1 | 0 | 0 | 0 |
| <u>5</u> | 0 | 1 | 0 | 1 | 0 |
| <u>6</u> | 0 | 1 | 1 | 0 | 1 |
| <u>7</u> | 0 | 1 | 1 | 1 | 1 |
| <u>8</u> | 1 | 0 | 0 | 0 | 0 |
| <u>9</u> | 1 | 0 | 0 | 1 | 0 |
| <u>10</u> | 1 | 0 | 1 | 0 | 1 |
| <u>11</u> | 1 | 0 | 1 | 1 | 1 |
| <u>12</u> | 1 | 1 | 0 | 0 | 1 |
| <u>13</u> | 1 | 1 | 0 | 1 | 0 |
| <u>14</u> | 1 | 1 | 1 | 0 | 1 |
| <u>15</u> | 1 | 1 | 1 | 1 | 0 |

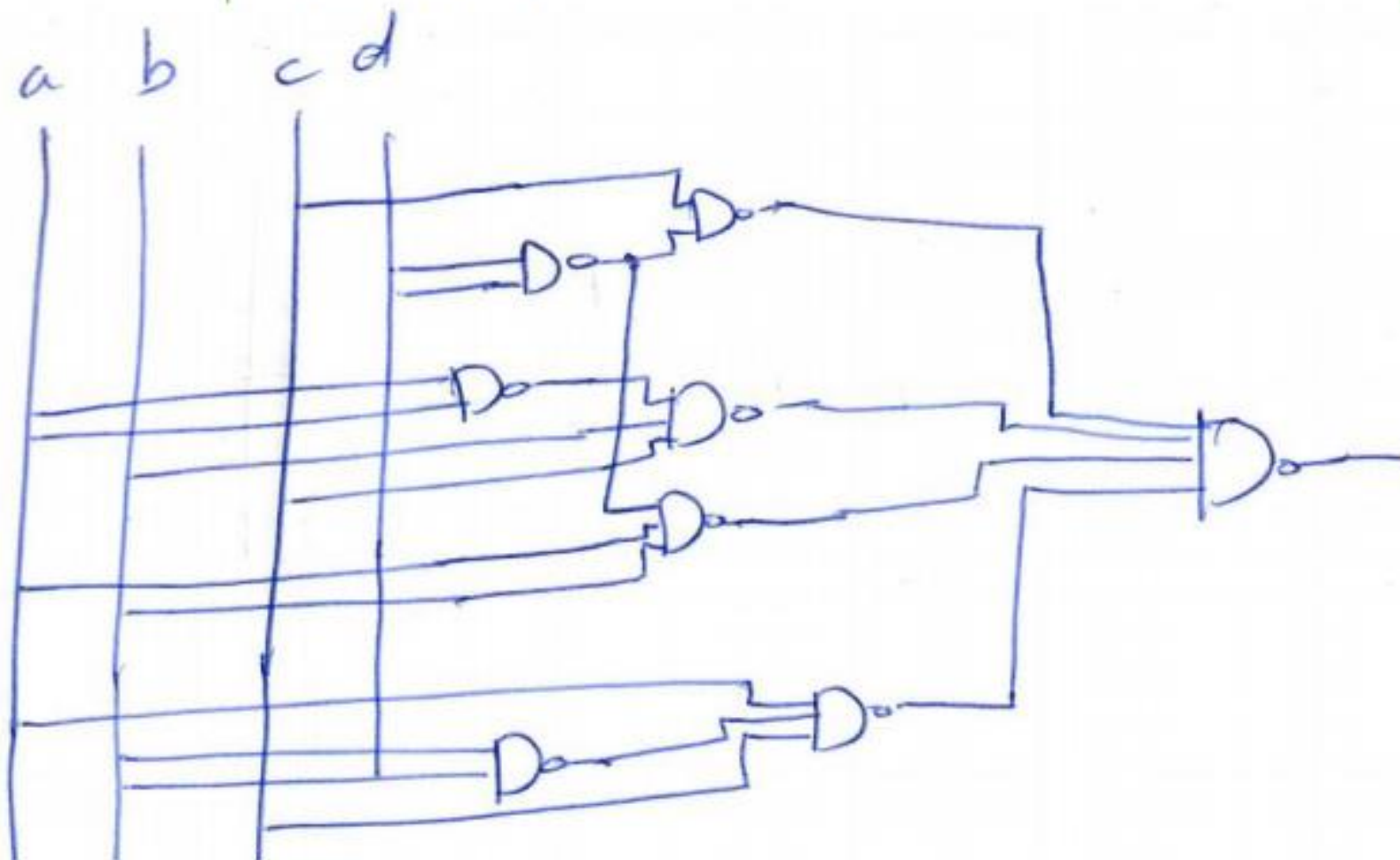
$$\Sigma G(a,b,c,d) = \Sigma a/c + \Sigma b/c + \Sigma a/bd + abd$$

$$G(a,b,c,d) = (a+c)(b+c)(a+b+d)(\Sigma a + \Sigma b + \Sigma d)$$

Exo 6

$$G(a,b,c,d) = c\bar{d} + \bar{a}bc + ab\bar{d} + a\bar{b}c$$

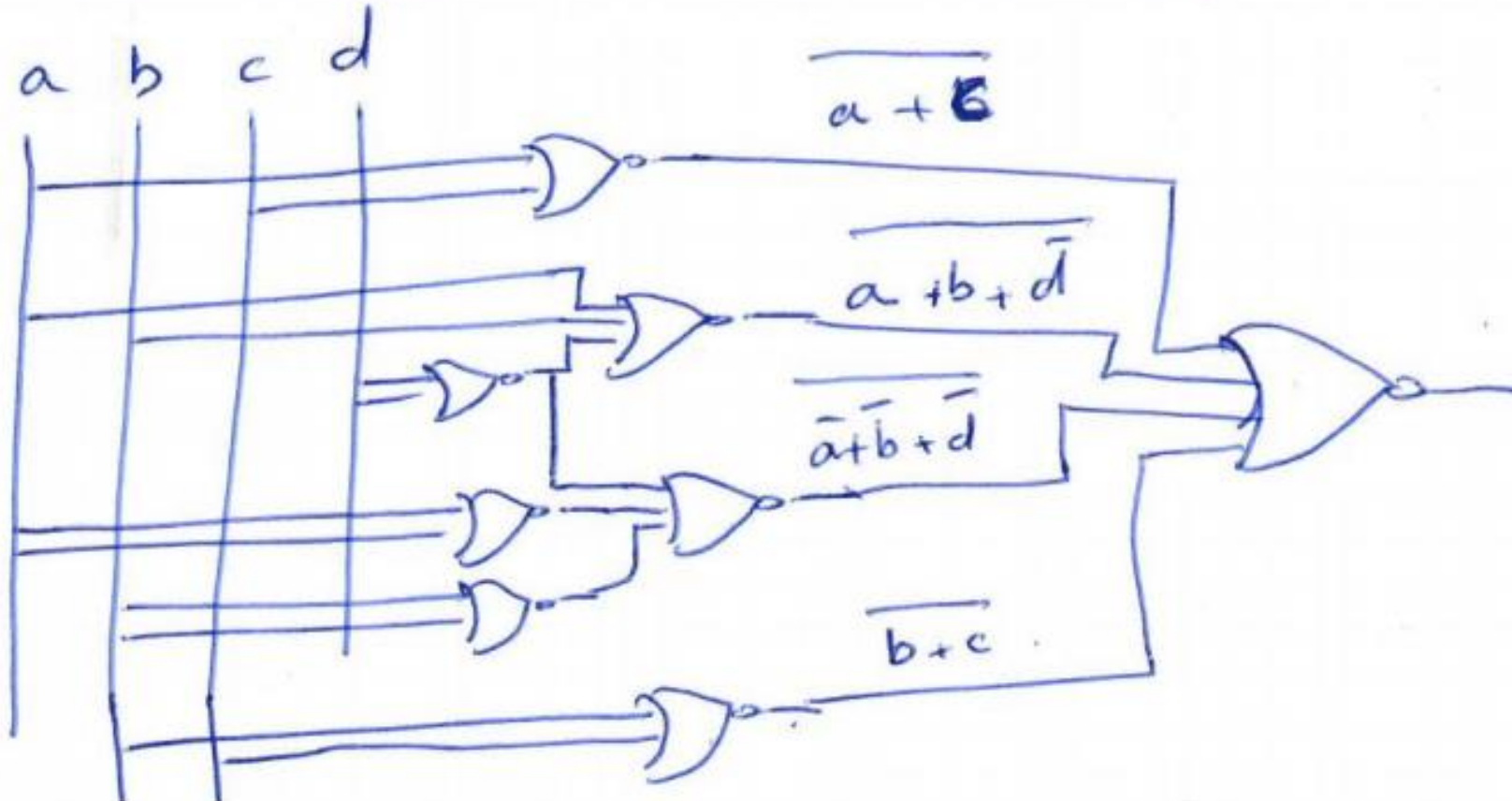
$$G(a,b,c,d) = \overline{c\bar{d} \cdot \bar{a}bc \cdot ab\bar{d} \cdot a\bar{b}c}$$



Exo 6 $G(a,b,c,d) = \overline{a}c + \overline{a}b\overline{d} + abd + \overline{b}c$

$$G(a,b,c,d) = (a+c)(a+b+\overline{d})(\overline{a}+\overline{b}+\overline{d})(b+c)$$

$$G(a,b,c,d) = \overline{\overline{(a+c)} + \overline{(a+b+\overline{d})} + \overline{(\overline{a}+\overline{b}+\overline{d})} + \overline{(b+c)}}$$



Exo 7

$$F = \overline{\overline{(x + y + z)} + (\overline{x + y + \bar{z}}) + \overline{\bar{x} + y + z}}$$

$$F = \overline{\overline{(x + y + z)} \overline{(\overline{x + y + \bar{z}})} \overline{\bar{x} + y + z}}$$

$$F = (x + y + z)(x + y + \bar{z})(\bar{x} + y + z)$$

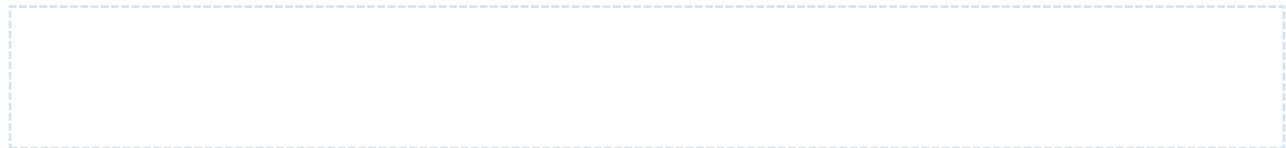
| x | y | z | $x + y + z$ | $x + y + \bar{z}$ | $\bar{x} + y + z$ | F |
|-----|-----|-----|-------------|-------------------|-------------------|-----|
| 0 | 0 | 0 | 0 | 1 | 1 | 0 |
| 0 | 0 | 1 | 1 | 0 | 1 | 0 |
| 0 | 1 | 0 | 1 | 1 | 1 | 1 |
| 0 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 0 | 0 | 1 | 1 | 0 | 0 |
| 1 | 0 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 0 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 |

| xy | 00 | 01 | 11 | 10 |
|-------|----|----|----|----|
| z = 0 | 0 | 1 | 1 | 0 |
| z = 1 | 0 | 1 | 1 | 1 |

$$F = y + xz$$

$$F = \overline{\overline{y + xz}} = \overline{\overline{y} \overline{xz}}$$

| x | y | z | F |
|---|---|---|---|
| 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 |
| 0 | 1 | 0 | 1 |
| 0 | 1 | 1 | 1 |
| 1 | 0 | 0 | 0 |
| 1 | 0 | 1 | 1 |
| 1 | 1 | 0 | 1 |
| 1 | 1 | 1 | 1 |



Exo 7

Soit la fonction $F(A,B,C)$ définie comme suit:

$F(A,B,C) = 1$ si $(ABC)_2$ comporte un nombre impair de 1;

$F(A,B,C) = 0$ sinon.

Etablir la table de vérité de F

| A | B | C | F |
|-----|-----|-----|-----|
| 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 1 |
| 0 | 1 | 0 | 1 |
| 0 | 1 | 1 | 0 |
| 1 | 0 | 0 | 1 |
| 1 | 0 | 1 | 0 |
| 1 | 1 | 0 | 0 |
| 1 | 1 | 1 | 1 |

$$F = \bar{a}\bar{b}c + \bar{a}b\bar{c} + a\bar{b}\bar{c} + abc$$

$$F = \bar{a}(\bar{b}c + b\bar{c}) + a(\bar{b}\bar{c} + bc)$$

$$F = \bar{a}(b \oplus c) + a(\overline{b \oplus c}) = a \oplus b \oplus c$$

